Advanced Topic in Modern Mathematical Sciences Lecturer: Hiroshi Matsuzawa Self Check Sheet No.02

| Student No. | Name | |
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- 1. Let $U \subset \mathbb{R}^N$ and T > 0. Write the definition of the parabolic boundary of $(0,T) \times U$.
- 2. What condition on the solutions guarantee that the uniqueness of the initial value problem of the heat equation when $U = \mathbb{R}^N$?
- 3. Weite the statement of the weak maximum principle for the parabolic equations.
- 4. Write the statement of the strong maximum principle for the parabolic equations (please choose one from the lecture note).
- **5**. Prove Theorem 4.2 for the case where f = f(x, u) is bounded and continuous and f_u is continuous.